

Calculus II, Section 7.6, #44
Integration Using Tables and Computer Algebra Systems

Use a computer algebra system to evaluate the integral. Compare the answer with the result using tables. If the answers are not the same, show that they are equivalent.¹

$$\int \frac{1}{\sqrt{1 + \sqrt[3]{x}}} dx$$

As we write this, it is January 26, 2016. Nobody uses tables to integrate any longer. We'll use Wolfram|Alpha (W|A).

Using Mathematica format, the input is

`Integrate[1/Sqrt[1+x^(1/3)], x]`

and we get

$$\int \frac{1}{\sqrt{1 + \sqrt[3]{x}}} dx = \frac{2}{5} \sqrt{\sqrt[3]{x} + 1} (3x^{2/3} - 4\sqrt[3]{x} + 8) + \text{constant}$$

Computed by Wolfram|Alpha

Thus,

$$\int \frac{1}{\sqrt{1 + \sqrt[3]{x}}} dx = \frac{2}{5} \sqrt{1 + \sqrt[3]{x}} (3x^{2/3} - 4\sqrt[3]{x} + 8) + C$$

¹Stewart, *Calculus, Early Transcendentals*, p. 513, #44.