

Calculus II, Section 7.6, #20
Integration Using Tables and Computer Algebra Systems

Use the Table of Integrals in your textbook to evaluate the integral.¹

$$\int \frac{\sin(2\theta)}{\sqrt{5 - \sin(\theta)}} d\theta$$

As we write this, it is January 26, 2016. Nobody uses tables to integrate any longer. We'll use Wolfram|Alpha (W|A).

For the input, we'll use x as the variable because for W|A, it is easier to type than θ . Using Mathematica format, the input is

`Integrate[Sin[2*x]/Sqrt[5-Sin[x]],x]`

and we get

$$\int \frac{\sin(2x)}{\sqrt{5 - \sin(x)}} dx = \frac{1}{3} \left(-4 \sqrt{5 - \sin(x)} \sin(x) - 40 \sqrt{5 - \sin(x)} + 40 \sqrt{5} \right) + \text{constant}$$

`Integrate[Sin[2*x]/Sqrt[5-Sin[x]],x] | Computed by Wolfram|Alpha`

Thus,

$$\int \frac{\sin(2\theta)}{\sqrt{5 - \sin(\theta)}} d\theta = \frac{1}{3} \left(-4 \sin(\theta) \sqrt{5 - \sin(\theta)} - 40 \sqrt{5 - \sin(\theta)} + 40 \sqrt{5} \right) + C$$

Since $40\sqrt{5}$ is a constant, another acceptable form is

$$= -\frac{4}{3} \sin(\theta) \sqrt{5 - \sin(\theta)} - \frac{40}{3} \sqrt{5 - \sin(\theta)} + C$$

and we can factor to get

$$= -\frac{4}{3} \sqrt{5 - \sin(\theta)} (\sin(\theta) + 10) + C$$

¹Stewart, *Calculus, Early Transcendentals*, p. 513, #20.